

The first test for this course will be given in class on Monday, September 29. It covers Chapter 1, Sections 1 through 8 of the textbook. (Since some people in the class have not seen recursion in a programming class, you will not be tested on Section 9.)

*The test will include some “short essay” questions that ask you to define something, or discuss something, or explain something, and so on. Other than that, you can expect most of the questions to be similar to problems that have been given on the homework. You can expect to do a few simple proofs, both formal proofs and more informal mathematical proofs. This might well include a proof by contradiction. You will **not** be asked to write a proof by induction, but you might have to answer questions about what it is or why it works.*

Here are some terms and ideas that you should be familiar with for the test:

translations from logic to English, and from English to logic

ambiguities in English

propositional logic

proposition

compound proposition

the logical constants $\mathbb{T}$ and $\mathbb{F}$

the logical and ($\wedge$), or ($\vee$), and not ($\neg$) operators

the or ($\vee$) operator is an “inclusive or”

truth table

logical equivalence ($\equiv$)

the conditional or “implies” operator ($\rightarrow$)

equivalence of $p \rightarrow q$ with $(\neg p) \vee q$

“the statement $p \rightarrow q$ makes no claim in the case when p is false”

the negation of $p \rightarrow q$ is equivalent to $p \wedge \neg q$

the biconditional operator ($\leftrightarrow$)

tautology

Boolean algebra

laws of Boolean algebra (double negation, De Morgan’s laws, distributive laws)

logic circuits and logic gates

AND, OR, and NOT gates

circuits that compute the value of compound propositions

converse of an implication

contrapositive of an implication

logical equivalence of an implication and its contrapositive

predicate logic

predicate

one-place predicate, two-place predicate, etc.

entity

domain of discourse

quantifiers, “for all” ($\forall$) and “there exists” ($\exists$)

using *variables* with predicates and quantifiers

negation of a statement that uses quantifiers

the difference between $\forall x \exists y$ and $\exists y \forall x$

arguments, valid arguments, and deduction

premises and conclusion of an argument

formal proof

how to show that an argument is invalid

logical implication ($\implies$)

Modus Ponens, Modus Tollens, and Syllogism

fallacies

mathematical proof

hypotheses

doing a “ $\forall x(P(x) \rightarrow Q(x))$ ” proof

doing an “if and only if” proof

existence proof

counterexample

proof by contradiction

the integers, $\mathbb{Z}$

the natural numbers, $\mathbb{N}$ (the non-negative integers)

the rational numbers, $\mathbb{Q}$ (can be written as a quotient of integers)

the real numbers, $\mathbb{R}$ (all numbers on the number line; decimal numbers)

irrational number (real number that is not rational such as π or $\sqrt{2}$)

divisibility (for integers n and m , m divides n if $n = km$ for some integer k)

prime number (only positive integer divisors are itself and 1)

even and odd numbers

Principle of Mathematical Induction, First Form and Second Form

proof by induction

why induction works

induction and falling dominoes

base case

inductive case

induction hypothesis