LAB 1

MATH 130 Section 2

January 18, 2018

Due January 22, 2018 at 11:15am

Covering Precalculus

Group Member 1: _______ Group Member 2: _______

YOU MUST SHOW ALL WORK TO RECEIVE CREDIT. Simplify your answers so that you have gathered all like terms, cancelled where possible, and so that there are no negative exponents or fractions within fractions in your final answer. Neatness is a plus!

This lab contains some exercises that represent situations that show up in the middle of calculus problems. Some ask you to solve for a variable, and some ask you merely to simplify an expression. Simplifying and canceling can be incredibly helpful in making a complex problem more tractable. You should look for opportunities to do so, and always check your work!

1. Simplify each of these expressions writing a single power of x.

$$(a)\frac{\sqrt{x^8}}{2x^2} = \frac{x^4}{2x^2}$$
$$= \frac{\chi^2}{2} \quad \text{or} \quad \frac{1}{2}\chi^2$$

(b)
$$\left(\frac{x^{3/5}}{x^{-2}}\right)^4 = \frac{x^{3/5} \cdot 4}{x^{-2} \cdot 4} = \frac{x^{12/5}}{x^{-8}} = x^{12/5} \cdot x^8 = x^{12/5} + \frac{40}{5} = x^{52/5}$$

2. (a) What is the definition of a rational function?

A rational function is a function R(x) that can be expressed as

a ratio of two polynomials, P(x) and Q(x), so that

$$R(x) = \frac{P(x)}{Q(x)}.$$

(b) Simplify this rational function: $\frac{9(x-2)^3(x+1)-2(x-2)^4(x-1)^2}{(x-2)^6}$.

$$= \frac{(x-2)^3 \left[9(x+1) - 2(x-2)(x-1)^2 \right]}{(x-2)^6} = \frac{(x-2)^3 \left[9x+9-2(x-2)(x^2-2x+1) \right]}{(x-2)^3 (x-2)^3}$$

$$= \frac{9x+9-2(x^3-2x^2+x-2x^2-4x-2)}{(x-2)^3} = \frac{-2x^3+8x^2+15x+13}{(x-2)^3}$$

3. Find the domain of $h(x) = \sqrt{\frac{x}{x-1}}$ and express your answers in interval notation. Be sure to explain your reasoning.

Eliminate zeros in the denominator: $x-1 \neq 0 \Rightarrow x \neq 1$

Domain: (-00,0] U (1,00)

4. Find **ALL** solutions of |5x - 7| = 13.

$$5x-7 = 13$$
 or $5x-7 = -13$
 $5x = -6$
 $x = 4$ $x = -\frac{6}{5}$

Solutions:
$$X = 4$$
 or $\frac{-6}{5}$

5. Give in interval notation in the simplest possible form the set of x for which $\frac{4x+3}{(x+1)} \le 1$. (Hint: When solving inequalities and equations with more than one term, begin by rewriting it with zero on one side.)

$$\frac{4x+3}{x+1} - 1 \le 0$$

$$\frac{3x+2}{x+1} + + + 0 - - 0 + + +$$

$$\frac{4x+3 - (x+1)}{x+1} \le 0$$

$$\frac{3x+2}{x+1} = 0$$

$$\frac{3x+2}{x+1} \le 0$$

$$\frac{3x+2}{x+1} \le 0$$

$$3x+2 = - - 0 + + + +$$

$$\frac{3x+2}{x+1} \le 0$$

$$3x+2 = - - - 0 + + + +$$

- 6. You will very soon need to use much of the information you already know about lines, their slopes and their equations. Here are several problems that you should be able to do quickly. If you are feeling rusty on terminology, check out Appendix A.
 - (a) Find an equation of the line through the point (3,4) that has slope $-\frac{1}{2}$.

$$y-4 = -\frac{1}{2}(x-3)$$

$$y = -\frac{1}{2}x + \frac{3}{2} + 4$$

$$y = -\frac{1}{2}x + \frac{11}{2}$$

(b) Find an equation of the line that passes through the points (-1,3) and (2,7).

$$m = \frac{7-3}{2-(-1)} = \frac{4}{3}$$

$$y - 7 = \frac{4}{3}(x-2)$$

$$y = \frac{4}{3}x - \frac{8}{3} + 7$$

$$y = \frac{4}{3}x + \frac{13}{3}$$

(c) Find an equation of the line parallel to 3x - 2y = 7 and passing through the point (-2, 2). Leave your final answer in slope-intercept form. (Hint: find the slope of the given line.)

parallel to
$$3x-2y=7 \Rightarrow$$
 has the same slope $3x-2y=7 \Rightarrow -2y=7-3x \Rightarrow y=\frac{3}{2}x-\frac{7}{2}$
Hence $m=\frac{3}{2}$.

Thus the line through $(-2,2)$ with slope $m=\frac{3}{2}$ is $y-2=\frac{3}{2}(x+2)$
 $y=\frac{3}{2}x+3+2$
 $y=\frac{3}{2}x+5$

7. Suppose $g(x) = \frac{2}{x-1}$ and $h \neq 0$. Find the following and simplify your solution as much as possible. (Leaving it in factored form is fine. Note that both x and h are variables here.)

(a)
$$g(-33)$$

$$g(-33) = \frac{2}{-33-1} = \frac{2}{-34} = -\frac{1}{17}$$

(b)
$$g(x+h)$$

$$g(x+h) = \frac{2}{(x+h)-1}$$
 or $\frac{2}{x+h-1}$

(c)
$$\frac{g(x+h)-g(x)}{h} = \frac{2}{x+h-1} - \frac{2}{x-1} = \frac{2(x-1)-2(x+h-1)}{(x+h-1)(x-1)}$$

$$= \frac{2x-2-2x-2h+2}{h(x-1)(x+h-1)}$$

$$= \frac{-2h}{h(x-1)(x+h-1)} = \frac{-2}{(x-1)(x+h-1)}$$

8. Factor the following polynomial as much as possible: $4x^7 - 64x^3$

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$$4x^{7} - 64x^{3} = 4x^{3} (x^{4} - 16)$$

$$= 4x^{3} (x^{2} + 4)(x^{2} - 4)$$

$$= 4x^{3} (x^{2} + 4)(x + 2)(x - 2)$$