Homework Week 5

MATH 204: Linear Algebra Due September 29, 2017 by 1:55pm

Remember that although you may discuss this assignment with others, your write up should be your own. Do not share your write-up, look at other's write-ups, discuss word for word how something should be proved, etc. Be sure to note with whom you collaborate if you do collaborate.

1. Number 12 from Section 1.7, page 62.

2. Number 38 from Section 1.7, page 62. (Hint: Try proof by contraposition!)

3. Determine whether each of the following transformations is linear. Justify your conclusions.

(a)
$$T: \mathbb{R}^2 \to \mathbb{R}^3$$
 defined by $T\left(\begin{bmatrix} x_1 \\ x_2 \end{bmatrix}\right) = \begin{bmatrix} x_2 \\ x_1 \\ x_1 + 2x_2 \end{bmatrix}$.

(b)
$$T: \mathbb{R}^3 \to \mathbb{R}^2$$
 defined by $T\left(\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}\right) = \begin{bmatrix} x_1^2 \\ x_3 \end{bmatrix}$.