

## MATH 2001 FIRST PROOF

**Homework.** Due Monday, February 8 at 6pm.

- Begin a new Overleaf document using the Proof Portfolio Template found on the course website.
  - Course website: [http://math.colorado.edu/~thga2182/Discrete\\_math/16S/](http://math.colorado.edu/~thga2182/Discrete_math/16S/)
  - Under the Resources heading, click on the Overleaf link next to ‘Proof portfolio template’.
  - Copy the template for the Proof Portfolio into a new file, and send me the Read & Edit link to your file.

**Exercise 1.** Write a new definition of *set equality* that involves explicit statements regarding the elements in the sets.

**Definition.**

**Exercise 2.** Suppose  $A$  and  $B$  are sets, and  $A = B$ . What can you say specifically about the elements in  $A$  and  $B$ ?

**Exercise 3.** Suppose  $A$  and  $B$  are sets. What would you have to do to prove that  $A = B$ ?

**Exercise 4.** Write a new definition of *subset* that involves explicit statements regarding the elements in the sets.

**Definition.**

**Exercise 5.** Suppose  $A$  and  $B$  are sets, and  $A \subseteq B$ . What can you say specifically about the elements in  $A$  and  $B$ ?

**Exercise 6.** Suppose  $A$  and  $B$  are sets. What would you have to do to prove that  $A \subseteq B$ ?

**Exercise 7.** Prove the following theorem.

**Theorem.** *If  $A$  and  $B$  are sets, and  $A = B$ , then  $A \subseteq B$ .*

*Proof.*

□