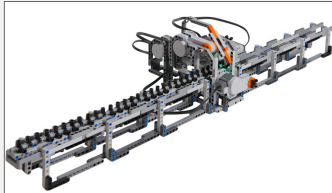
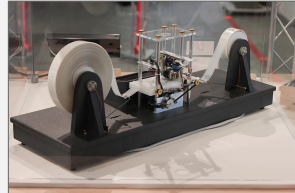


Physical Turing Machines



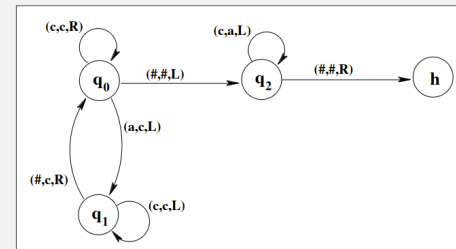
LEGO Turing Machine
<https://www.youtube.com/watch?v=FTSAIF9AHN4>



from the 2012 GO ASK A.L.I.C.E. exhibition at Harvard University's Collection of Historical Scientific Instruments
https://commons.wikimedia.org/wiki/File:Turing_Machine_Model_Davey_2012.jpg

Computing Functions

Definition 5.2. Suppose that Σ and Γ are alphabets that do not contain $\#$ and that f is a function from Σ^* to Γ^* . We say that f is **Turing-computable** if there is a Turing machine $M = (Q, \Lambda, q_0, \delta)$ such that $\Sigma \subseteq \Lambda$ and $\Gamma \subseteq \Lambda$ and for each string $w \in \Sigma^*$, when M is run with input w , it halts with output $f(w)$. In this case, we say that M **computes** the function f .



$\Sigma = \{ a \}$
 computes $f(a^n) = a^{2n}$