

My Office Hours: M & W 2:30–4:00, Tu 2:00–3:30, & F 1:30–2:30 or by appointment. **Math**

Intern: Sun: 2:00–5:00, 7:00–10pm; Mon thru Thu: 3:00–5:30 and 7:00–10:30pm in Lansing 310.

Website: <http://math.hws.edu/~mitchell/Math131F15/index.html>.

☛ Practice

- Review** L'Hopital's Rule in Section 4.7 and the online notes. More interesting ones have the form $0 \cdot \infty$, 0^0 , ∞^0 , 1^∞ , and $\infty - \infty$.
 - Read** all of 7.7 on improper integrals which we continue to discuss next time.
- Suggested last time. l'Hôpital's's Rule: Try page 307ff #13, 19–31(odd), 49, 53, 55, 65.
 - Interesting ones of the form $0 \cdot \infty$, 0^0 , ∞^0 , 1^∞ , and $\infty - \infty$. Page 307ff #45, 49, 53, 55, 65, and 67.

Hand In

These should be quick. Some are WeBWork problems. Potential answers: k , k^2 , 0 , 1 , 2 , $1/2$, $1/4$, $\ln 2$, $\ln 3$, e^2 , e^{-2} , diverges, e .

- Start WeBWork Day27—many of these are the same as the hand in problems—and finish Day26.
- Evaluate these limits using L'Hôpital's Rule when appropriate. In part (b), k is a non-zero constant. Use correct limit notation.

$$(a) \lim_{x \rightarrow 0^+} x^2 \ln x \text{ WeBWork} \quad (b) \lim_{x \rightarrow \infty} x \tan\left(\frac{1}{x}\right) \text{ WeBWork} \quad (c) \lim_{x \rightarrow \infty} \left(1 - \frac{2}{x}\right)^x \text{ WeBWork}$$

$$(d) \lim_{x \rightarrow 0} \frac{\sin kx}{\arcsin x} \quad (e) \lim_{x \rightarrow 0^+} x^{3x} \text{ WeBWork} \quad (f) \lim_{x \rightarrow \infty} \ln(2x - 2) - \ln(x + 7) \text{ WeBWork}$$

- Page 578 #6. Use correct limit notation. Similar to a WeBWork problem.

3. Determine $\int_0^\infty \frac{4}{\sqrt[3]{x+1}} dx$. Use correct limit notation. Similar to a WeBWork problem.

4. Determine $\int_0^\infty 2xe^{-x^2} dx$. Use correct limit notation.

5. Determine $\int_0^\infty \frac{4}{1+x^2} dx$. Use correct limit notation.

- Suppose that a tank is formed by rotating the region in the first quadrant enclosed by $y = (x + 2)^2$, the y -axis, and the x -axis about the y -axis (see Figure 1).

Just set up the integral for the work done pumping the oil ($D = 60 \text{ lbs/ft}^3$) to a height 3 feet above the top of the tank if there is only 1 foot of oil in the tank.

- BONUS:** Determine $\lim_{x \rightarrow 0^+} (\tan x)^x$. Hint: Use the "log process." After applying L'Hôpital's Rule the first time, simplify and apply again. (Also a WeBWork Bonus problem.)

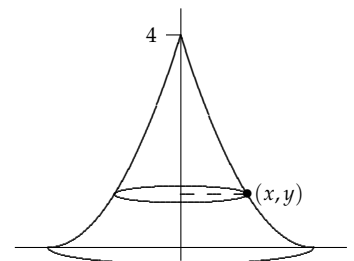


Figure 1: The circular cross-section formed by rotating the point (x, y) about the y -axis.