

Complex Motion

Complex Motion

Motion means that the position changes over time.

We'll consider two patterns of how the position is changed –

- by updating the position
 - add or subtract some amount from the previous x, y to get the new x, y
- by computing the position outright
 - have some formula to compute x, y directly

These ideas are not limited to motion – any value (size, color, etc) can be updated/computed in the same ways.

Updating Position

new position = old position + speed × time interval

- we usually take the time interval to be one frame so this simplifies to

new position = old position + speed

- or, when updating animation variables

$position = position + speed$

- instead of adding or subtracting depending on the direction of movement, treat speed as positive or negative

- positive → moving right ($xspeed$) or down ($yspeed$)
- negative → moving left ($xspeed$) or up ($yspeed$)

which is implemented as

$x = x + xspeed$
 $y = y + yspeed$

Steady Motion

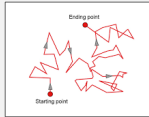
$position = position + speed$

- for steady motion, the speed is constant so we typically don't bother with variables for speed (e.g. $x = x+1$)

Random Walk

$$\text{position} = \text{position} + \text{speed}$$

- the speed doesn't have to be constant
- for a *random walk*, use a small random number for the speed
 - `random(8)` – a float between 0 and 8, but not including 8 itself
 - `random(-5,10)` – a float between -5 and 10, but not including 10 itself
 - `int(random(-5,10))` – an int between -5 and 10, but not including 10 itself
- random walks are a good simulation of *Brownian motion*, the random movement of particles in a liquid or gas as they get bumped by individual molecules or atoms



Speeding Up and Slowing Down

$$\text{position} = \text{position} + \text{speed}$$

- the speed can itself change over time

What changes? position *and* speed

- need animation variables for both
- *acceleration* is the rate of change of speed
 - often constant, so no need for an acceleration animation variable
 - can be in the same direction as speed → speeding up
 - same sign
 - can be in the opposite direction of speed → slowing down (deceleration)
 - opposite sign

$$\begin{aligned}\text{position} &= \text{position} + \text{speed} \\ \text{speed} &= \text{speed} + \text{acceleration}\end{aligned}$$

Physically-Based Motion Simulation

$$\begin{aligned}\text{position} &= \text{position} + \text{speed} \\ \text{speed} &= \text{speed} + \text{acceleration}\end{aligned}$$

How do we change the speed in a realistic way?

Elements –

- *gravity* is acceleration downwards
 - only affects yspeed
 - positive number because positive speed means moving downwards
 - $\text{yspeed} = \text{yspeed} + g$ ($g > 0$)
- *air resistance* is deceleration proportional to speed
 - amount depends on speed, in opposite direction
 - $\text{speed} = \text{speed} - k * \text{speed}$ ($k \geq 0, k \ll 1$)

<< means "much less than"
>> means "much greater than"

Physically-Based Motion Simulation

$$\begin{aligned}\text{position} &= \text{position} + \text{speed} \\ \text{speed} &= \text{speed} + \text{acceleration}\end{aligned}$$

Additional elements –

- *bouncing* is changing direction to go the other way when a surface is hit
 - sometimes bounce, sometimes don't means ...?
 - on-the-spot "to do or not to do" – `if (have hit) { do the bounce }`
 - "going the other way" = change the sign of xspeed when a vertical wall is hit, change the sign of yspeed when a horizontal wall is hit
 - $\text{speed} = -1 * \text{speed}$
- *damping* is energy lost due to friction when bouncing
 - object doesn't bounce as high each time
 - $\text{speed} = -k * \text{speed}$ instead of $\text{speed} = -1 * \text{speed}$ ($k < 1, k \gg 0$)

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