## Finite-State Automata and Regular Languages

**Theorem 3.5.** The intersection of two regular languages is a regular language.

The union of two regular languages is a regular language.

The concatenation of two regular languages is a regular language.

The complement of a regular language is a regular language. The Kleene closure of a regular language is a regular language.

## sketch of proof

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- build DFAs or NFAs accepting the languages using Theorem 3.3
- build a DFA or NFA using those DFAs/NFAs which accepts the union/concatenation/complement/Kleene closure
- for two DFAs  $M_1$ ,  $M_2$ , M accepting  $M_1 \cap M_2$  contains pairs of states from  $M_1$  and  $M_2$  – the idea is to move through  $M_1$ ,  $M_2$  simultaneously and only accept strings which end in final states in both machines
- corresponding to that DFA/NFA

## • for a DFA M, M' accepting the complement of M's language is M with the final and non-final states switched use Theorem 3.4 to conclude that there is a regular expression

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- the idea is to move through  $M_1$ ,  $M_2$  simultaneously and only accept strings which end in final states in both machines



Finite-State Automata and Regular Languages • for a DFA M, M' accepting the complement of M's language is M with the final and non-final states switched – must have all transitions specified, no omit-trap-state shortcuts!