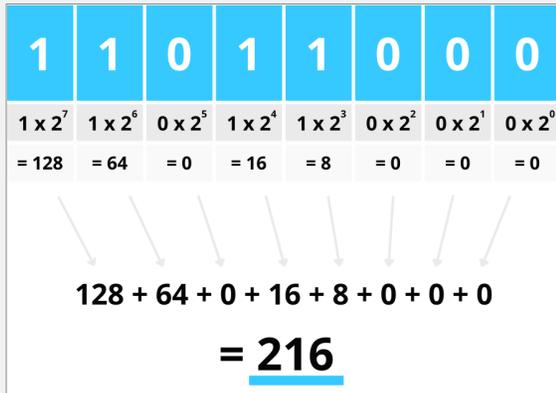


## Binary Numbers



## Bit Strings as Sets



- a bit string can also be interpreted as a set
  - associate each position with an element of the set
  - treat 1 as “in” and 0 as “not in”
- integer types in Java
  - byte – 8 bits
  - short – 16 bits
  - int – 32 bits
  - long – 64 bits

## Bitwise Operators

Operators	Description	Use
&	Bitwise AND	op1 & op2
	Bitwise OR	op1   op2
^	Bitwise Exclusive OR	op1 ^ op2
~	Bitwise Complement	~op
<<	Bitwise Shift Left	op1 << op2
>>	Bitwise Shift Right	op1 >> op2

### Bitwise AND

Binary Representation of 10 = 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0

Binary Representation of 2 = 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0

Binary Representation of a&b = 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0

### Bitwise OR

Binary Representation of 10 = 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0

Binary Representation of 2 = 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0

Binary Representation of a|b = 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0

## Bitwise Operators

Operators	Description	Use
&	Bitwise AND	op1 & op2
	Bitwise OR	op1   op2
^	Bitwise Exclusive OR	op1 ^ op2
~	Bitwise Complement	~op
<<	Bitwise Shift Left	op1 << op2
>>	Bitwise Shift Right	op1 >> op2

### Bitwise One's Complement

Binary Representation of 10 = 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0

Binary Representation of ~a = 1 1 1 1 1 1 1 1 1 1 1 1 0 1 0 1

## Shift Operators

Operators	Description	Use
&	Bitwise AND	op1 & op2
	Bitwise OR	op1   op2
^	Bitwise Exclusive OR	op1 ^ op2
~	Bitwise Complement	~op
<<	Bitwise Shift Left	op1 << op2
>>	Bitwise Shift Right	op1 >> op2

Binary Representation of 8 = 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0

Binary Representation of a<<b = 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0

Binary Representation of 8 = 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0

Binary Representation of a>>b = 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0

## Set Operations

- bitwise | corresponds to set union
- bitwise & corresponds to set intersection
- to test whether  $x$  is in  $A$  –  
 $(A \& x) \neq 0$
- adding an element –  $A \cup \{x\}$   
 $A | x$
- removing an element –  $A \setminus \{x\}$   
 $A \& \sim x$
- generating  $\{x\}$  where  $x$  is the element in position  $pos$   
 $1 \ll pos$

## Hexadecimal

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

$101010110111_2 = 0xAB7$

1. Suppose that the numbers  $x$  and  $y$  represent the sets  $A$  and  $B$ . Show that the set  $A \setminus B$  is represented by  $x \& (\sim y)$ .

2. Write each of the following binary numbers in hexadecimal:  
 a)  $10110110_2$       b)  $10_2$       c)  $111100001111_2$       d)  $101001_2$

3. Write each of the following hexadecimal numbers in binary:  
 a)  $0x123$       b)  $0xFADE$       c)  $0x137F$       d)  $0xFF11$

4. Give the value of each of the following expressions as a hexadecimal number:  
 a)  $0x73 | 0x56A$       b)  $\sim 0x3FF0A2FF$   
 c)  $(0x44 | 0x95) \& 0xE7$       d)  $0x5C35A7 \& 0xFF00$   
 e)  $0x5C35A7 \& \sim 0xFF00$       f)  $\sim(0x1234 \& 0x4321)$

# Applications

```
String source = e.getSource().getClass().getName();
int mod = e.getModifiers();

if ((mod & ActionEvent.ALT_MASK) > 0) {
}

if ((mod & ActionEvent.SHIFT_MASK) > 0) {
}

if ((mod & ActionEvent.META_MASK) > 0) {
}

if ((mod & ActionEvent.CTRL_MASK) > 0) {
}
```

event handling in Java Swing

```
function printInformation (): void {
  const info: any = {
    firstName: 'Hendrik',
    lastName: 'Erz',
    affiliation: 'Linköping University',
    occupation: 'PhD Student'
  }
  console.log(`${info.firstName} ${info.lastName}, ${info.occupation} (${info.affiliation})`)
}
```

```
const FIRST_NAME = 1
const LAST_NAME = 2
const OCCUPATION = 4
const AFFILIATION = 8
```

```
function printInformation (which: number): void {
  const info: any = {
    firstName: 'Hendrik',
    lastName: 'Erz',
    occupation: 'PhD Student',
    affiliation: 'Linköping University'
  }
  if (which & FIRST_NAME) {
    console.log(info.firstName)
  }
  if (which & LAST_NAME) {
    console.log(info.lastName)
  }
  if (which & OCCUPATION) {
    console.log(info.occupation)
  }
  if (which & AFFILIATION) {
    console.log(info.affiliation)
  }
}
```

```
printInformation(FIRST_NAME | LAST_NAME)
printInformation(OCCUPATION | LAST_NAME)
```

```
const SHORT_OCC = LAST_NAME | OCCUPATION
// ... snip ...
if (which & SHORT_OCC === SHORT_OCC) {
  console.log(`${info.lastName}, ${info.occupation}`)
  return
}
```

# Applications

- Linux file permissions

```
$ ls -l
drwxr-xr-x. 4 root root 68 Jun 13 20:25 tuned
-rw-r--r--. 1 root root 4017 Feb 24 2022 vimrc
```

- File type: -
- Permission settings: **rw-r--r--**
- Extended attributes: dot (.)
- User owner: **root**
- Group owner: **root**

- rw- user
- r-- group
- r-- other

```
$ chmod ug+rxw example.txt
$ chmod o+r example2.txt
chmod o-rwx example.txt
```

```
chmod 644 example.txt
```

- octal
- r (read): 4
  - w (write): 2
  - x (execute): 1

# Applications of Bitwise Operations

- extracting RGB color components
  - RGB color is stored as a 32-bit integer

```
rgb = 0xff8000;
b = rgb & 0xff;
g = (rgb >> 8) & 0xff ; // g contains 80
r = (rgb >> 16) & 0xff ; //r contains ff
```

- top 8 bits are used for transparency (alpha)

---

9. Java, C, and C++ each have a boolean data type that has the values *true* and *false*. The usual logical and, or, and not operators on boolean values are represented by the operators `&&`, `||`, and `!`. C and C++ allow integer values to be used in places where boolean values are expected. In this case, the integer zero represents the boolean value *false* while any non-zero integer represents the boolean value *true*. This means that if  $x$  and  $y$  are integers, then both  $x \& y$  and  $x \&\& y$  are valid expressions, and both can be considered to represent boolean values. Do the expressions  $x \& y$  and  $x \&\& y$  always represent the same boolean value, for any integers  $x$  and  $y$ ? Do the expressions  $x | y$  and  $x || y$  always represent the same boolean values? Explain your answers.