Improving Map/Dictionary

- unsorted leads to O(1) insert/delete but O(n) search for both arrays and linked lists
- sorted leads to differences between arrays and linked lists
 - O(log n) search and O(n) delete for arrays
 - O(n) search and O(1) delete for linked lists

Can we do better?

CPSC 327: Data Structures and Algorithms . Spring 2025

CPSC 327: Data Structures and Algorithms . Spring 2025

- O(n) delete in arrays is due to shifting can't do much about that
 - circular arrays worked for queues because insert/delete was only at the ends
- can we exploit the sorted order to improve searching in linked lists?
 - like binary search in arrays, perhaps...

Doing Better 8 15 20 5 11 4 16 each middle element only needs to store the location of two other middle elements \rightarrow binary tree structure left and right overall the elements are ordered. ٦Z so the "other middle elements" are $\overline{\mathcal{N}}^{6}$ smaller and larger than the "middle $\overline{\mathcal{N}}$ element", respectively -> binary search tree

http://cslibrary.stanford.edu/110/BinaryTrees.html

Improving an Implementation – Map

Binary search exploits the sorted order – but it requires efficient random access.

Or does it?

- the first iteration of binary search requires knowing the middle element
- successive iterations require knowing the middle element of one of the halves

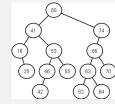
Finding the middle element is achieved in arrays by arithmetic involving array indexes, but what if we just stored the necessary info instead?

• store instead of computing...

CPSC 327: Data Structures and Algorithms . Spring 2025

Binary Search Trees

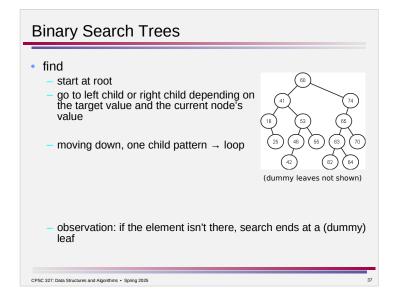
- a binary tree with an ordering property for the elements
 - for every node, all of the elements in the left subtree are less than or equal to the node's element and all of the elements in the right subtree are greater than the node's element



(dummy leaves not shown)

- operations
 - find
 - insert
- remove
- visit all elements (traverse) in order

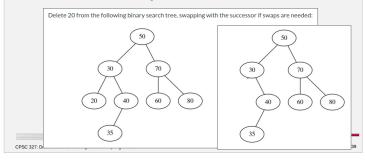
CPSC 327: Data Structures and Algorithms • Spring 2025

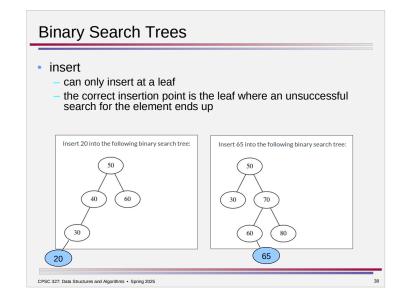


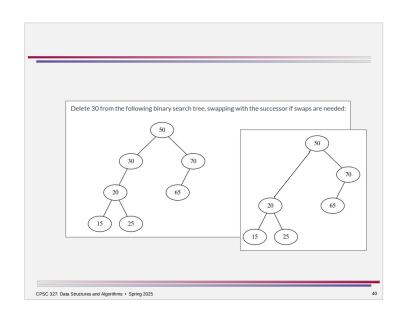
Binary Search Trees

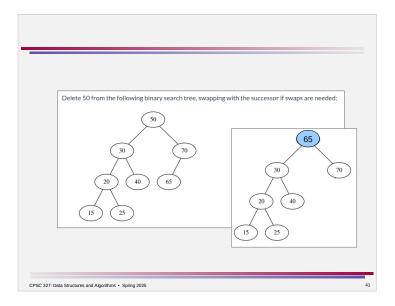
remove

- can only remove above a leaf
- if the element to remove does not have at least one leaf child, swap it with a safe element which does has at least one leaf child
 - i.e. the next element larger or smaller than the one to remove









Implementing Map

CPSC 327: Data Structures and Algorithms • Spring 2025

- can store (key,value) pairs in a binary search tree ordered by key
 - let h be the height of the tree
 - all operations are O(h) as it may be necessary to go from the root all the way down to a leaf

