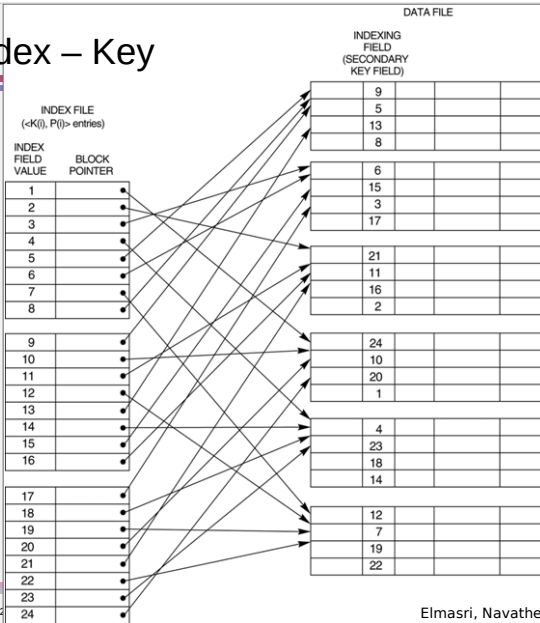


Secondary Index – Key

indexing field is a key –

one index record per data record

index record points to data block containing that record



Secondary Index – Key

indexing field is a key
one index record per data record

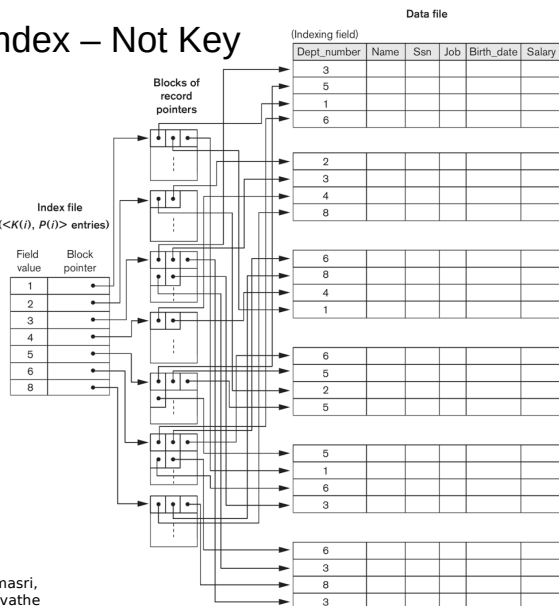
operation	method	# blocks accessed	file properties		
			# records	r	30,000
search on indexing field	linear search on file	max $b = 3000$ avg $b/2 = 1500$	block size	B	1024
	binary search on index + data block	$\text{ceil}(\log_2(b_i)) + 1 = 9 + 1 = 13$	record length	R	100 bytes (fixed length)
range search on indexing field	linear search on file	$b = 3000$	blocking factor (# records per block)	$bfr = \text{floor}(B/R)$	10
	using index (binary search on index to find first, then scan index to determine data blocks for the rest of the s matches)	$\text{ceil}(\log_2(b_i)) + \text{ceil}(s/bfr_i) + s = 9 + \text{ceil}(s/68) + s$ note that if $s \geq b$ (or even close to b), it is better to just scan the file	# data blocks	b	$b = \text{ceil}(r/bfr)$ 3000
			index properties		
			ordering key length	V	9 bytes
			block pointer	P	6 bytes
			# index records	r_i	one per data record 30,000
			index record length	R_i	$R_i = V + P$ 15 bytes
			blocking factor for index	bfr_i	$bfr_i = \text{floor}(B/R_i)$ 68
			# index blocks	b_i	$b_i = \text{ceil}(r_i/bfr_i)$ 442

Secondary Index – Not Key

indexing field is not a key, using indirect blocks –

one index record per distinct value of the indexing field

index record points to *indirect block(s)* containing pointers to the data blocks containing the records with that value



Secondary Index – Non-Key (Indirect Blocks)

indexing field is not a key
one index record per distinct value + indirect blocks

file properties					
number of distinct values	d	3000	average # of records per distinct value	r_d	$r_d = r/d = 30000/3000 = 10$
index properties					
ordering key length	V				9 bytes
block pointer	P				6 bytes
# index records	r_i		one per distinct value		3000
index record length	R_i		$R_i = V + P$		15 bytes
blocking factor for index	bfr_i		$bfr_i = \text{floor}(B/R_i)$		68
# index blocks	b_i		$b_i = \text{ceil}(r_i/bfr_i)$		45
blocking factor for indirect blocks	bfr_b		$bfr_b = \text{floor}(B/P)$		170
average # indirect blocks per index record			$\text{ceil}(r_d/bfr_b)$		$\text{ceil}(10/170) = 1$
total # indirect blocks	b_b		average # indirect blocks per index record $\times r_i$		3000

Secondary Index – Non-Key (Indirect Blocks)

indexing field is not a key
one index record per distinct value + indirect blocks

operation	method	# blocks accessed
search on indexing field	linear search on file	$b = 3000$
	binary search on index + indirect block(s) + data block(s) (expect r/d records to match value)	$\text{ceil}(\log_2(b_i)) + \text{average \# indirect blocks per index record} + \text{ceil}(r/d) = 6+1+10 = 17$
range search on indexing field	linear search on file	$b = 3000$
	using index (find first using binary search on index, then scan index to get rest of the s matches, loading indirect block(s) for each, then retrieving the data block as each record is identified)	$\text{ceil}(\log_2(b_i)) + \text{ceil}(s/r_d/bfr) + s/r_d \times \text{average \# indirect blocks per index record} + s = 6+s/680+s/10+s$ if $s \geq b$ (and even somewhat less), better off just scanning the file

$d = \# \text{ distinct values}$
 $s = \# \text{ matches}$

An equality search using a single-level index with r_i index records and b_i blocks would require reading, on average, how many index blocks?

1		0%	
log bi	6 respondents	100%	✓
bi/2		0%	
bi		0%	
log ri		0%	
ri/2		0%	
ri		0%	
it depends on the number of records and/or blocks in the file		0%	
it depends on the kind of index (primary, clustering, or secondary)		0%	
none of the above		0%	

the index records for all indexes are ordered by the indexing field
→ can be searched with binary search

An equality search in a file with r records and b blocks using a single-level index would require reading, on average, how many data blocks? s is the number of matched records.

1		0%	
s/bfr	2 respondents	33%	
s	1 respondent	17%	
log b		0%	
b/2		0%	
b		0%	
log r		0%	
r/2	1 respondent	17%	
r		0%	
it depends on the kind of index (primary, clustering, or secondary)	2 respondents	33%	✓
none of the above		0%	

how the matching data records are distributed amongst the data records depends on the ordering of the file records relative to the ordering of the index records

Multilevel Index

If there are lots of records, there could be a lot of index blocks and searching them all could take some time.

- index the index!

The first level index is one of the single-level indexes.

The second level index is a primary index on the first-level index.

- first level index is an ordered file with records containing just an ordering key value and block pointer(s) – and no duplicates

The third level index is a primary index on the second-level index...

...until the index at a particular level requires only one block.

Multilevel Index

Searching –

- read one block at each level
- read the final data block(s)

Range searching –

- search for the first value down to the first-level index
 - read one block at each level
- scan the first-level index to find all the matching index records
- read the data blocks indicated by the first-level index records

Indexing Recap

Three possible index organizations:

- primary – ordered by same field(s) as file, and field(s) are a key
- clustering – ordered by same field(s) as file, but field(s) not a key
- secondary – ordered by different field(s) than file

Performance:

- $O(\log_2 b_i + s)$ for searching on indexing field(s)
 - s = number of matching records
- primary is better than clustering is better than secondary
 - but there can be at most one primary or clustering index per file
- multilevel index reduces search time from $O(\log_2 b_i)$ to $O(\log_{b_{fr_i}} b_i)$
- indexes are less beneficial for small tables and queries that match most of the rows