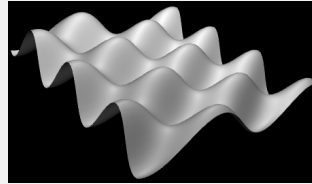
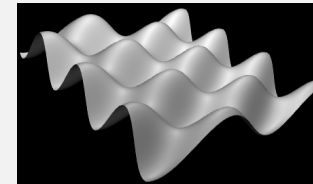


Modeling – Surfaces

- parametric surfaces
 - defined by a function $f(u,v)$
 - the surface consists of all points $f(u,v)$ for u, v in the range 0-1
- steps
 - define a function with parameters u, v which returns the (x,y,z) point defined by u, v
 - create a `ParametricGeometry` using that function
 - slices and stacks determine the number of subdivisions in each direction
 - create a `Mesh` with that geometry and the desired material
 - creates a mesh approximating the surface from $f(u,v)$ values for a grid of points $0 \leq u, v \leq 1$



Modeling – Parametric Surfaces



refers to the import map

```
<script type="importmap">
{
  "imports": {
    "three": "../threejs/three.module.min.js",
    "addons/": "../threejs/"
  }
}
</script>
```

```
import {ParametricGeometry} from "addons/geometries/ParametricGeometry.js";
```

```
function surfaceFunction( u, v, vector ) {
  let x,y,z; // Coordinates for a point on the surface,
             // calculated from u,v, where u and v
             // range from 0.0 to 1.0.
  x = 20 * (u - 0.5); // x and z range from -10 to 10
  z = 20 * (v - 0.5);
  y = 2 * (Math.sin(x/2) * Math.cos(z));
  vector.set( x, y, z );
}
```

define the function

error in book – no THREE, as ParametricGeometry is not part of the three.js core

```
var surfaceGeometry = new ParametricGeometry(surfaceFunction, 64, 64);
var surface = new THREE.Mesh( surfaceGeometry, material );
```

create a ParametricGeometry
create a Mesh from the geometry

Modeling – Curves

- parametric curves
 - defined by a function $f(t)$
 - the curve consists of all points $f(t)$ for t in the range 0-1
- steps
 - define a function with a parameter t which returns either a point (x,y) (2D curve) or a point (x,y,z) (3D curve)
 - create a `Curve`
 - set the curve's `getPoint` property to the function

```
var helix = new THREE.Curve();
helix.getPoint = function(t) {
  var s = (t - 0.5) * 12*Math.PI;
  // As t ranges from 0 to 1, s ranges from -6*PI to 6*PI
  return new THREE.Vector3(
    5*Math.cos(s),
    s,
    5*Math.sin(s)
  );
}
```

note that a curve is not itself a geometry, but it can be used to generate a geometry

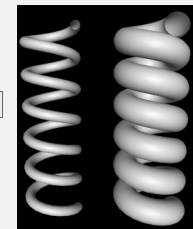
Modeling – Surfaces From Curves

- tube geometries

```
tubeGeometry1 = new THREE.TubeGeometry( helix, 128, 2.5, 32 );
```

- parameters

- a `Curve` object (requires a 3D curve)
- number of subdivisions along the length of the curve
- radius of the circular cross-section of the tube
- number of subdivisions around the circumference of the cross-section of the tube

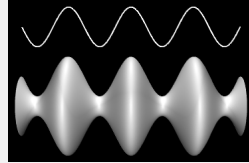


- then create a `Mesh` with that geometry and the desired material

- creates a mesh approximating the surface from $f(t)$ values for points $0 \leq t \leq 1$

Modeling – Surfaces From Curves

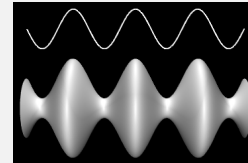
- lathing – rotate curve about a line to generate a surface of rotation
- steps
 - define a Curve (2D)
 - generate a set of points along the curve
 - create a LatheGeometry using those points



```
new THREE.LatheGeometry( points, slices )
```

- rotates the curve around the y axis (the curve's points are in the xy plane)
- parameters
 - points – array of Vector2
 - slices – number of subdivisions around the circle of rotation
- create a Mesh with that geometry and the desired material
 - creates a mesh approximating the surface from $f(t)$ values for points $0 \leq t \leq 1$

Modeling – Surfaces From Curves



```
var cosine = new THREE.Curve();
cosine.getPoint = function(t) {
    t = (t - 0.5) * 7*Math.PI;
    return new THREE.Vector2( 3 + 2*Math.cos(t), t );
}
```

define 2D curve

```
var points = cosine.getPoints(128);
var latheGeometry = new THREE.LatheGeometry(points, 32);
var lathe = new THREE.Mesh(latheGeometry, material);
scene.add(lathe);
```

get points

create LatheGeometry

create a Mesh from the geometry

add the object to the scene

Modeling – Surfaces From Curves

- extruding – move a filled 2D shape along a path through space



- steps
 - create a shape defining the (closed) curve
 -
 - create an ExtrudeGeometry using that shape
 - create a Mesh with that geometry and the desired material
 - creates a mesh approximating the surface

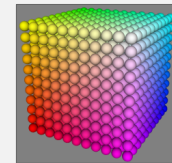
```
var path = new THREE.Shape();
path.moveTo(0,10);
path.bezierCurveTo( 0.5, 20, -10, 0, -10 );
path.bezierCurveTo( -20, -10, 0.5, 0, 10 );
```

see the 2D Canvas API in section 2.6.2 for how to work with these shapes

```
var extrudeGeom1 = new THREE.ExtrudeGeometry( path, {
    curveSegments: 32, // How many points on each part of the path
    amount: 6, // size in the 3rd dimension; how far to extrude.
    bevelSize: 1,
    bevelThickness: 1 } // or bevelEnabled: false to not bevel the edges
);
var extrude1 = new THREE.Mesh(extrudeGeom1, material);
```

Other Modeling

- InstancedMesh
 - for a number of objects with the same geometry but different transformations and (possibly) material color
 - see section 5.3.1



Cubemaps

```
let textureURLs = [ // URLs of the six faces of the cube map
  "cubemap-textures/park/posx.jpg", // Note: The order in which
  "cubemap-textures/park/negx.jpg", // the images are listed is
  "cubemap-textures/park/posy.jpg", // important!
  "cubemap-textures/park/negy.jpg",
  "cubemap-textures/park/posz.jpg",
  "cubemap-textures/park/negz.jpg"
];

/**
 * Loads a list of textures. If a callback function is provided, it is
 * called once after all textures are loaded. This is used to load a
 * set of six textures to use on the six faces of the cube in the first
 * scene.
 */
function loadTextures(textureURLs, callback) {
  let loaded = 0;
  function loadedOne() {
    loaded++;
    if (callback && loaded == textureURLs.length) { // all textures have been loaded
      callback();
    }
  }
  /* A function that will be called if the attempt to load the texture fails. */
  function textureError() {
    document.getElementById("message").innerHTML = "Error: Failed to load texture.";
  }
  let textures = new Array( textureURLs.length );
  for (let i = 0; i < textureURLs.length; i++) {
    let tex = new THREE.TextureLoader().load( textureURLs[i], loadedOne, textureError );
    textures[i] = tex;
  }
  return textures;
}
```

- to apply a cubemap to the outside of a box, texture each face separately

```
/* Load the six image textures and create the six face materials. */
let textures = loadTextures(textureURLs, render);
let materials = [];
for (let i = 0; i < 6; i++) {
  materials.push( new THREE.MeshPhongMaterial( {
    color: "white",
    map: textures[i]
  } ) );
}
```

```
/* Create a cube with the six textures on the six faces of the cube. */
cube = new THREE.Mesh( new THREE.BoxGeometry(20,20,20), materials );
scene.add(cube);
```

Reflection via Environment Mapping

- steps

- load a cubemap texture

```
var textureURLs = [ // URLs of the six faces of the cube map
  "cubemap-textures/park/posx.jpg", // Note: The order in which
  "cubemap-textures/park/negx.jpg", // the images are listed is
  "cubemap-textures/park/posy.jpg", // important!
  "cubemap-textures/park/negy.jpg",
  "cubemap-textures/park/posz.jpg",
  "cubemap-textures/park/negz.jpg"
];
```

```
var texture = new THREE.CubeTextureLoader().load( textureURLs );
```

- for the skybox, set the scene's background to the cubemap texture

```
scene.background = texture;
```

- for the reflective object, create a MeshBasicMaterial

- set the material's envMap property to the cubemap texture object

```
var material = new THREE.MeshBasicMaterial( {
  color: "white", // Color will be multiplied by the environment map.
  envMap: texture // Cubemap texture to be used as an environment map.
} );
```

Reflection via Environment Mapping

- dynamic cubemaps can be generated using THREE.CubeCamera

- <https://threejs.org/docs/#api/en/cameras/CubeCamera>

Refraction via Environment Mapping

- steps

- load a cubemap texture
 - specify that the cubemap is to be used for refraction

```
var textureURLs = [ // URLs of the six faces of the cube map
  "cubemap-textures/park/posx.jpg", // Note: The order in which
  "cubemap-textures/park/negx.jpg", // the images are listed is
  "cubemap-textures/park/posy.jpg", // important!
  "cubemap-textures/park/negy.jpg",
  "cubemap-textures/park/posz.jpg",
  "cubemap-textures/park/negz.jpg"
];

texture = new THREE.CubeTextureLoader().load( textureURLs );
texture.mapping = THREE.CubeRefractionMapping;
```

Refraction via Environment Mapping

- steps, continued

- for the skybox, set the scene's background

```
scene.background = texture;
```

- for the refractive object, create a MeshBasicMaterial
 - set the material's envMap property to the cubemap texture object
 - set other material properties
 - refractionRatio – ratio of index of refraction of air to material (1 = no bending of light, smaller values = greater bending – default is 0.98)
 - reflectivity – proportion of light transmitted (< 1 to make object look cloudy)

```
var material = new THREE.MeshBasicMaterial( {
  color: "white",
  envMap: texture,
  refractionRatio: 0.6
} );
```

Shadow Mapping in three.js

- steps

- enable shadow computations in the renderer
 - expensive, so disabled by default
- enable casting of shadows for each light
 - only applicable to DirectionalLights and SpotLights
- enable casting and receiving of shadows for each object
 - "receiving" means shadows will be visible on that object
- configure the view volumes of the shadow cameras
 - directional lights use OrthographicCamera
 - spotlights use PerspectiveCamera
- (optionally) increase the size of the shadow map
 - larger map increases accuracy of the shadows

```
renderer.shadowMap.enabled = true;
```

```
light.castShadow = true;
```

```
object.castShadow = true;
object.receiveShadow = true;
```

```
light.shadow.mapSize.width = 1024;
light.shadow.mapSize.height = 1024;
```

Shadow Mapping in three.js

- configuring the shadow camera view volume

- light.shadow.camera is the shadow camera for light
- for directional lights (orthographic camera), properties are left, right, bottom, top, near, far
- for spotlights (perspective camera), properties are fov, near, far
 - fov is the field of view angle, in degrees (should match spotlight's cutoff angle)
- values are in view coordinates
- view volume should be big enough to include all of the objects that cast shadows, but not too big
 - too big impacts the accuracy of the shadow map

Other three.js Topics

- mouse interaction – covered section 5.3.2
 - OrbitControls and TrackballControls
 - clicking on objects within the scene
- keyboard input (key presses)
 - not directly covered in the textbook, but present in many of the examples in chapter 5
- custom shaders

Custom Shaders

- steps
 - write GLSL vertex and fragment shaders
 - three.js provides a number of built-in uniforms and attributes
 - create a `ShaderMaterial` which specifies the shader programs and the values for custom (not built in) parameters

Built-in Uniforms and Attributes

- | | |
|---|--|
| <ul style="list-style-type: none">• vertex shader<ul style="list-style-type: none">– uniforms<ul style="list-style-type: none">• <code>modelMatrix</code>• <code>modelViewMatrix</code>• <code>projectionMatrix</code>• <code>viewMatrix</code>• <code>normalMatrix</code>• <code>cameraPosition (WC)</code>– attributes<ul style="list-style-type: none">• <code>position</code>• <code>normal</code>• <code>uv</code> | <ul style="list-style-type: none">• fragment shader<ul style="list-style-type: none">– uniforms<ul style="list-style-type: none">• <code>viewMatrix</code>• <code>cameraPosition</code> |
|---|--|

reference:
<https://threejs.org/docs/#api/en/renderers/webgl/WebGLProgram>

ShaderMaterial

- key properties
 - vertexShader
 - fragmentShader
 - uniforms
 - for custom uniforms
 - (custom attributes are set as part of the geometry)

reference:
<https://threejs.org/docs/#api/en/materials/ShaderMaterial>
<https://threejs.org/docs/#api/en/materials/Material>

Example

```
<script type="x-shader/x-vertex" id="vshader_silhouette">
void main() {
    vec4 coords = vec4(position,1.0)+vec4(.03*normal,0);
    vec4 ec = modelViewMatrix * coords;
    gl_Position = projectionMatrix * ec;
}
</script>

<script type="x-shader/x-fragment" id="fshader_silhouette">
void main () {
    gl_FragColor = vec4(0.0,0.0,0.0,1.0);
}
</script>
```

black silhouette

```
silhouetteMaterial = new THREE.ShaderMaterial( {
    vertexShader: getTextureContent("vshader_silhouette"),
    fragmentShader: getTextureContent("fshader_silhouette"),
    side: THREE.BackSide
} );
```

```
<script type="x-shader/x-vertex" id="vshader_silhouette">
void main() {
    vec4 coords = vec4(position,1.0)+vec4(.03*normal,0);
    vec4 ec = modelViewMatrix * coords;
    gl_Position = projectionMatrix * ec;
}
</script>

<script type="x-shader/x-fragment" id="fshader_silhouette">
uniform vec3 color;

void main () {
    gl_FragColor = vec4(color,1.0);
}
</script>
```

silhouette with a specified color

```
silhouetteMaterial = new THREE.ShaderMaterial( {
    uniforms : {
        color: { value: new THREE.Color( 0x000000 ) }
    },
    vertexShader: getTextureContent("vshader_silhouette"),
    fragmentShader: getTextureContent("fshader_silhouette"),
    side: THREE.BackSide
} );
```

getTextureContent is a local utility function to get the text from an HTML element

Working With Lights in Shaders

- UniformsLib defines a bunch of uniforms that can get passed to your shaders

```
lights: {
    ambientLightColor: { value: [] },
    lightProbe: { value: [] },
    directionalLights: { value: [], properties: {
        direction: {},
        color: {},
        shadow: {},
        shadowBias: {},
        shadowRadius: {},
        shadowMapSize: {}
    } },
}
```

(a small section)

reference:
<https://threejs.org/docs/#api/en/renderers/shaders/UniformsLib>

Working With Lights in Shaders

```
<script type="x-shader/x-vertex" id="vshader">
varying vec3 v_coords; // EC
varying vec3 v_normal; // EC

void main() {
    vec4 coords = vec4(position,1.0);
    vec4 ec = modelViewMatrix * coords;
    gl_Position = projectionMatrix * ec;

    v_coords = ec.xyz;
    v_normal = normalize(normalMatrix*normal);
}
</script>
```

need EC point and normal for lighting calculations

Working With Lights

```
struct DirectionalLight {
    vec3 color;
    vec3 direction;
};

uniform vec3 diffuseColor;
uniform vec3 specularColor;
uniform float specularExponent;

uniform vec3 ambientLightColor;
uniform DirectionalLight directionalLights[ NUM_DIR_LIGHTS ];

varying vec3 v_color; // EC
varying vec3 v_normal; // EC
```

circled items match the UniformLibs definition
NUM_DIR_LIGHTS is also automatically defined

```
lights: {
    ambientLightColor: { value: [] },
    lightProbe: { value: [] },
    directionalLights: { value: [], properties: {
        direction: {},
        color: {},
        shadow: {},
        shadowBias: {},
        shadowMapSize: {}
    } }
},
```

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```
<script type="x-shader/x-fragment" id="fshader">
    struct DirectionalLight {
        vec3 color;
        vec3 direction;
    };

    uniform vec3 diffuseColor;
    uniform vec3 specularColor;
    uniform float specularExponent;

    uniform vec3 ambientLightColor;
    uniform DirectionalLight directionalLights[ NUM_DIR_LIGHTS ];

    varying vec3 v_color; // EC
    varying vec3 v_normal; // EC

    vec3 lightingEquation( DirectionalLight light,
                           vec3 eyeCoords, // Eye coordinates for the point.
                           vec3 N, // Normal vector to the surface.
                           vec3 V // Direction to viewer.
                           ) {
        vec3 reflection = vec3(0);

        vec3 L, R; // Light direction and reflected light direction.
        L = normalize( light.direction );

        if (dot(L,N) <= 0.0) { // Light does not illuminate the surface
            return reflection;
        }
        reflection += dot(L,N) * light.color * diffuseColor;

        R = -reflect(L,N);
        if (dot(R,V) > 0.0) { // ray is reflected toward the viewer
            float factor = pow(dot(R,V),specularExponent);
            reflection += factor * specularColor * light.color;
        }

        return reflection;
    }

    void main () {
        vec3 viewDirection = normalize(-v_color);
        vec3 color = vec3(0.0);
        color += ambientLightColor*diffuseColor;
        for (int i = 0; i < NUM_DIR_LIGHTS; i++) {
            color += lightingEquation( directionalLights[i],
                                     v_color, v_normal,
                                     viewDirection );
        }
        gl_FragColor = vec4(color,1.0);
    }
</script>
```

Working With Lights in Shaders

```
shaderMaterial = new THREE.ShaderMaterial( {
    uniforms: THREE.UniformsUtils.merge([
        THREE.UniformsLib['lights'],
        {
            diffuseColor: { value: new THREE.Color(0xffff00) },
            specularColor: { value: new THREE.Color(0x000000) },
            specularExponent: { value: 50.0 }
        }
    ]),
    vertexShader: getTextureContent("vshader"),
    fragmentShader: getTextureContent("fshader"),
    side: THREE.FrontSide,
    lights: true
} );
```

merge combines multiple sets of properties
provides the lights section from UniformsLib

must enable lighting in order for lighting info to be passed to shader

```
// create some lights and add them to the scene.
// dim light shining from above
scene.add( new THREE.DirectionalLight( 0x000000, 0.4 ) );
// a light to shine in the direction the camera faces
var viewpointLight = new THREE.PointLight( 0x000000, 0.8 );
viewpointLight.position.set(0,0,10); // shines down the z-axis
scene.add(viewpointLight);
shaderMaterial.needsUpdate = true;
```

set to true if adding or changing lights after shader is compiled

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