# Syllabus for MATH 135: First Steps into Advanced Mathematics

#### Fall Semester 2016

Professor: Erika L.C. King

Office: Lansing 304

Office Hours: M 1:30-3:30pm, W 12:30-2:00pm, Th 4:30-5:30pm, F 11:00am-Noon, and by appt.

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Class: held TTh: 10:20am-11:45am in Eaton 111

Textbook: Discrete Mathematics with Ducks, by sarah-marie belcastro

Website: http://math.hws.edu/eking/FirstSteps/math135.html

## Course Content and Organization

First Steps into Advanced Mathematics is primarily a language course. We will be learning the precise language that produces rigorous proofs and reveals the beauty of mathematics. In order to have some basic material to which we can apply this language, we will also learn some discrete mathematics. Discrete mathematics is the study of mathematical objects that are not continuous. Think of the difference between graphing the line y = x and graphing the set of all points (x, x) where x is an integer. The former is a graph of a continuous function, while the second is not; it is discrete. The goal is for you to use the language (often within the realm of discrete mathematics) to begin to produce mathematics, not just consume it. We will develop our production skills by studying the Counting and Proofs, Sets and Logic, Graphs and Functions, Induction, and Fun with Cardinality chapters of the text, as well as studying a mathematical structure called posets with outside materials. Exploring these topics will increase our abilities to create, read, write, speak, and present mathematics.

This class will likely be very different from your previous mathematics courses partly because it will be run in a seminar style. There will be discussions, daily student presentations, and small group work. Very little time will be spent in lecture. You will be expected to read and work with material **before** it is discussed in class. While previous courses may have challenged you to solve problems that were modifications of exercises seen before, here we begin to see that advanced mathematics requires more creativity. Here we begin to learn how to weave together sometimes seemingly unrelated facts in a logical way to create something new. Most students find both the format and the work for this class very challenging and engaging. I hope you will find the collaborative class sessions and office hours supportive and enlightening. While the course expectations may at first seem daunting, keep in mind that your classmates and I are embarking on this adventure with you. I think you will find the journey very rewarding (and even enjoyable!) as long as you stay involved.

# Goals and Prerequisites

The main goal of the course is for you to begin understanding how to discover and produce mathematics on your own. Here we also collect tools that will be used again in all upper level mathematics courses. These tools include the precise language of mathematics, many proof techniques, and some basic mathematical structures that will be invaluable throughout your mathematical career. By the end of the course you should know when to and how to apply the following proof techniques: direct, contrapositive, existence, uniqueness, contradiction, and induction. In addition,

you should be familiar with the following mathematical structures and operations: basic logic (including implications, logical equivalence, and quantification), basic set theory and set operations, relations on sets (especially equivalence relations and partial orders), basic combinatorics (including product and sum principles, basic graph structures and properties, and congruence modulo n), and functions and some of their properties (injective, surjective, bijective). By the end of the term you should be confident in your ability to read and write several different types of proof. Your mathematical vocabulary will have increased particularly with respect to the language of sets, relations, and functions. You should feel more confident in presenting mathematics, both orally in class and in written assignments. In short, you should feel prepared to embark on the study of higher-level mathematics.

In order to enroll for this class, you must have earned a C or better in MATH 131 (Calculus II) or earned AP credit for the class. This course is intended for students seriously considering becoming mathematics majors or minors. Since this is such a foundational course, I expect that this course will be top priority for you this semester. Indeed you should expect to spend at least 10 to 12 hours a week on this material outside of class. To reduce the amount of conscious time spent on this class, start assignments as soon as they are assigned! (You will be amazed at how much your mind can accomplish subconsciously if you give it the time!)

## Supplies

In addition to the usual pencils, erasers, and paper, you will need a composition book (spiral notebooks and three-ring binders will **not** be accepted) to use as a journal, and a highlighter. Your class notes should be kept in a different notebook (the type of your choosing) from your journal. Please also obtain access to a stapler (This does not require buying one. For example, there is a stapler available for use in the library for free.); collected work on more than one page should be stapled (not clipped) before submission. You should also have a colored pencil or pen for denoting revisions to your journal work.

#### Assessment

Reading and exercises will be assigned daily. Check the course website after each class for the assignment. These assignments will be divided into two types: journal assignments and collected assignments.

Journal Assignments: Journal assignments will be based on readings in the textbook and may include additional exercises not found in the text. Journal assignments should be completed before the beginning of the next class period.

Daily readings will usually only consist of a few pages, but should be carefully read several times. In your journal, keep a list of all new vocabulary (perhaps together at the back of your journal), and solve any assigned questions in or related to the reading. Also include any questions you have about the material. Leave a space after each question so that you can fill in the answer when you discover it in class or office hours. At least one question should be included with each assignment and it should be as specific as you can make it. So, for example, "What do they mean in Theorem 5?" is not very specific, whereas, "In Theorem 5, is the second hypothesis really necessary?" is. Trying to figure out what exactly does not make sense to us is sometimes a difficult task, but a vital one as we search for clarity. Asking questions is an important skill for mathematicians to have as it leads to the ability to create interesting research questions. Be ready to ask your question(s) on the reading at the beginning of each class.

I hope that you find this book enjoyable to read. Note that the duck symbols guide you. There are portions of the text you should **not** read until you have worked on the previous problems. Be sure to observe the ducks with the stop signs warning this. The opportunity for you to work through and discover ideas on your own is invaluable; do not deny yourself that! Working through the reading assignments is the most important part of this course. You are encouraged to find a partner or two with whom you work some of this material. You should always come to class prepared to discuss and present on the reading. Although it is important that you eventually understand all of the material, it is not important for you to have all the right answers when we first discuss it. What is important is that you have taken time to carefully think and work through the ideas, and to identify specific questions. Many of the exercises you tackle in your journal work will be discussed in class. Take time to go back and look at your previous work and note if your proofs and solutions were correct and if not, why not. You may find a different approach to a problem than one shown in class. Remember: there is often more than one right way. If your way was not correct, try to use your mistakes to help you understand the material better. Your journal work gives us the opportunity to focus on the more complex questions in class, and helps to guide you to be a more independent mathematician.

I will collect your journal three or four times during the semester (usually at each exam), but you should be working in your journal nearly every day. I will be looking for solutions/proofs to some of the exercises/theorems, but I will also be looking for overall effort put into exploring and engaging with the course material. Follow these guidelines to organize your journal work:

- Keep exercises in the order they are assigned.
- Clearly label each problem you are working on with its section and problem number.
- Use a highlighter to mark each label, so they are easily identifiable.
- If unable to fully complete a proof or problem, show attempts and why they did not work.
- Note with whom you worked (if anyone).
- Your journal should **not** contain class notes or collected assignments.

Collected Homework: Roughly twice a week you will turn in a written assignment: one due on Tuesday and one on Friday. These will ask you to demonstrate your ability to clearly and precisely express mathematical ideas in writing. This will include writing up proofs of theorems. Each proof will be assigned two grades – one grade for content and one grade for form. Content reflects your mastery of the mathematical concepts required for the proof and your use of appropriate proof methods. The grade for form will take into consideration clarity of expression, completeness, and proper usage of both English and mathematical grammar. In addition, **bonus** points will be given for **creative** approaches to proofs or multiple correct proofs. Those assignments due on Tuesdays will normally be shorter, due by 4PM in my office, and must be done **individually** without help from any other people or outside resources except your book, notes, and me. Treat them like a take home exam. Those assignments due on Fridays will usually be longer and may be turned in no later than 2PM in my office. You may choose a partner or two with whom you may discuss the assignments that are due on Fridays. Be sure to note on your assignment anyone with whom you worked. Even if you discuss Friday assignments with others, your write-up should be completed entirely on your own. Take notes while discussing ideas with your classmates, but decide on the final organization and wording of your write-up on your own. Your work should be your own expression. This means you should not share or have someone else look at your assignment before it is graded. All assignments should be turned in via paper and not email. Your work should be done neatly in pencil or typed. Note that while assignments are due outside of class, you are always welcome and encouraged to turn them in at the beginning of the class before they are due. The point value of each written assignment will be determined by the length and complexity of the assignment, and thus will vary. Assignments will be considered late if they are not turned in by the time and date they are due. You may turn in up to two late assignments (any time before Wednesday at 4pm, 24 hours after they are due, for Tuesday assignments; and any time before Sunday at 1pm, 47 hours after they are due, for Friday assignments) without penalty. Neat work (including stapling if more than one page, and no jagged-edged papers, in addition to neat writing or typed papers) will earn one bonus point. Keep your eyes open for opportunities to re-write work for which you did not earn full credit the first time.

Quizzes: Occasionally I may give short announced or pop quizzes to see if you are keeping up with the material. These quizzes will mainly ask you to give basic definitions and examples from topics in the reading and/or class discussions. I will let you use your journals for any pop quizzes, so be sure to keep up with the material and bring your journals to class. **Under no circumstances may a quiz be made up.** Quizzes will be worth 10 points.

Presentations: Much of the class will consist of students presenting their journal and class work to each other. You will be expected to do your share in this. Much of the time I will rely on volunteers to make presentations. This makes it possible for you to present the work about which you feel most confident. But the fact that so much of your understanding depends on this participation means that you must volunteer on a regular basis. Don't assume that because others volunteer, you (or your grade) are off the hook. I may also assign presentations ahead of time or call on students randomly. Some presentations will be less formal, but formal presentations should be at least as well prepared as written work. Like written assignments, presentations will be given a grade for mathematical content and a grade for the form and quality of the presentation. Given the size of the class, each student will likely only have time for one formal presentation. However, this requirement may increase depending on our movement through the material. The formal presentation will be worth 20 points.

The person who is presenting his or her work at the board is not the only person with responsibilities in a presentation. The students sitting at their desks have as central a role to play. They should be making clarifying suggestions, asking questions and adding comments. If I think there is clarification needed or that there is confusion about the topic at hand, I will likely ask questions of those seated rather than of the presenter.

In addition to individual presentations, there will be at least one formal group presentation. Occasionally, some groups may be assigned to present and other groups may be assigned to evaluate a specific presentation. These will be worth 30 points.

Seminars: In addition to regular class time, you will be required to attend two mathematics/computer science seminar talks during the semester, at least one of which must be on mathematics. Seminars usually begin between 3pm and 5pm and last an hour (the days vary). Attendance at each talk is worth 10 points (you must be present and attentive for the entire talk to receive full credit).

Bonus: You may earn 5 bonus points for each additional mathematics/computer science seminar talk you attend. You may earn a maximum of 15 bonus points from seminar talks. Up to 10 points can be earned for each additional presentation. There is no maximum for bonus points earned through presentations.

Bonus field assignments may also be offered several times throughout the semester. Field assignments are designed to give you opportunities to explore the breadth of the field of mathematics

and what it means to be a mathematician. The field assignments may involve readings taken from the book *Letters to a Young Mathematician* by Ian Stewart, a newspaper or journal article, or an assignment asking you to explore a mathematical review database. You will write a short paper for each assignment, and you may be asked to present your findings in class. Each paper will be worth 10 points, and will be evaluated for how well it is written as well as creativity and expression of thought. You will have roughly a week to complete these.

Active participation: Your journal, collected assignments, quizzes, presentations and seminar attendance will make up 50% of your grade.

Exams: There will be two **evening** midterm exams. The first will take place Wednesday, October 5th from 7:15pm until 9:15pm. The second midterm will be Tuesday, November 15th from 7:15pm until 9:15pm. Each midterm will be worth 15% of your course grade. The final exam will be Tuesday, December 13th from 8:30am until 11:30am. There will likely be a take-home group project portion of the final. The in-class and take-home finals together will be worth 20% of your course grade. It is impossible to construct fair makeup exams in mathematics. Thus, for your protection, my policy is that there are **no** makeup exams. **You must be present for all exams.** 

Attendance: Since your participation is such a large part of the class, absences will greatly affect your grade. More than two unexcused absences will lower your grade by at least one letter. The greater the number of absences, the greater the reduction. Excused absences require documentation such as a letter from a dean. Habitual tardiness will lower your grade. More than four absences will likely result in automatic failure. On the other hand, if you have perfect attendance in the course and no latenesses, I will add 3 points to your lowest exam. It is impolite to arrive late to class or leave the classroom while class is in session unless it is an emergency. Cell phones should be turned off and stowed during the entire class period.

#### Disclaimer

The above exam dates, quantity of graded work, policies, and course layout are subject to change in the event of extenuating circumstances.

## The Center for Teaching and Learning (CTL)

At Hobart and William Smith Colleges, we encourage you to learn collaboratively and to seek the resources that will enable you to succeed. The Center for Teaching and Learning (CTL) is one of those resources: CTL programs and staff help you engage with your learning, accomplish the tasks before you, enhance your thinking and skills, and empower you to do your best. Resources at CTL are many: Study Mentors help you find your time and manage your responsibilities, Writing Fellows help you think well on paper, and professional staff help you assess academic needs, to name a few. I encourage you to explore these and other CTL resources designed to inspire your very best work. You can talk with me about these resources, visit the CTL office on the 2nd floor of the library to discuss options with the staff, or visit the CTL website at http://www.hws.edu/academics/ctl/index.aspx.

If you are a student with a "disability" (or what I like to call a "nontraditional approach to learning") for which you may need accommodations, you should self-identify and register for services with the Coordinator of Disability Services at the CTL, and provide documentation of your disability. Disability-related accommodations and services will not be provided until the registration and documentation process is complete. The guidelines for documenting disabilities can be

found at the following website: http://www.hws.edu/academics/ctl/disability\_services.aspx. Please direct questions about this process, or Disability Services at HWS, to David Silver, Coordinator of Disability Services, at silver@hws.edu or x3351.

## **Academic Integrity**

I highly encourage you to form a small group with whom you can discuss some of the journal work and collaborative assignments. Verbalizing your questions, explaining your mathematical ideas and listening to others will increase your understanding. However, you should **not** feel free to copy someone else's work, ask someone else to edit your work, edit someone else's work, **or** make your work available to someone else. Copying constitutes plagiarism, a violation of academic integrity which could result in failure in the course. There is, of course, no collaboration or use of outside resources (including other textbooks and the internet) allowed on individual assignments, quizzes, in-class or take-home exams (unless specifically noted). Violation of the Colleges' Principle of Academic Integrity will likely result in a report sent to your file in the dean's office and/or appearance before the Committee on Standards.

#### How to Succeed

- Attend all classes on time.
- Do the reading and journal assignments carefully.
- Start assignments early so that you have time to work on the assignment several times and see me, if necessary.
- Spend some time each week working on the material from this class by yourself.
- Review the notes from the last class before coming to class again. Recopy the notes if appropriate. This makes preparation for a test easy.
- Participate in class discussions, and volunteer to present!
- Find one to three classmates with whom you can discuss the material outside of class.
- Ask your classmates and me lots of questions.
- Listen carefully to other students' ideas.
- Complete your write-ups on your own, including doing your own editing.
- Use my office hours liberally.
- Have fun!

### First Collected Homework

This assignment will contribute toward your active participation grade. Write a full one-page typed (usual font size and margin widths) autobiography. Discuss the following in your essay:

- whether you are planning on being a mathematics major or minor
- why you chose to take this course
- your favorite and least favorite memories of mathematics
- your favorite mathematical topic
- what you expect to learn in this course
- your favorite hobbies, and anything else interesting (for example, what you did over summer break).

The paper is due by 4:00pm tomorrow (Wednesday, August 31st) or before. You may hand it in personally to me, place it in the homework collection box if I have placed it outside my office door, or just slip it under my office door. This assignment also includes a short one-on-one meeting with me in my office after I have read your essay. Sign up for this appointment when you drop off your paper. Please bring a photo of yourself, with which you are willing to part, to the meeting (you do not need to have the photo when you turn in your essay). This meeting and the photo help me get to know each of you I do not, and catch up with those of you I do. Your grade on this assignment will be based on whether you address all the topics requested, as well as the quality of your writing (including good grammar and typography) and your prompt attendance at our meeting, photo in hand. It is critical that you are on time for your appointment! This assignment is worth 15 points. **Note:** if you had me for Calculus I and/or II in a previous semester you do not need to bring a photo, **but** you should make sure this essay is different from the essay(s) you gave me then. It should update any of the topics listed above that have changed or discuss further topics you think are especially important to who you are.