

## Collected Homework Week 13

MATH 278: Number Theory  
Due: April 22, 2015 at 4:00pm

Name (Print): \_\_\_\_\_

### 1. Chinese Remainders

- (a) Find three consecutive numbers such that the first is divisible by  $5^2$ , the second is divisible by  $3^3$ , and the third is divisible by  $2^4$ .
  - (b) Solve  $341x \equiv 521 \pmod{595}$ . (Note  $595 = 5 \cdot 7 \cdot 17$ .)
2. Write a proof of Theorem 4.3 from page 54 of our text.
  3. Write a proof of Theorem 4.4 from page 54 of our text.
  4. Solve exercise 4.20 on page 57 of our text.

## Notebook Problems Week 13

1. Write a proof of Theorem 4.2 from page 54 of our text.
2. Quickie: write a proof of Theorem 4.21 from page 57 of our text.
3. Prove that if  $p$  and  $q$  are distinct primes, then  $p^{q-1} + q^{p-1} \equiv 1 \pmod{pq}$ .