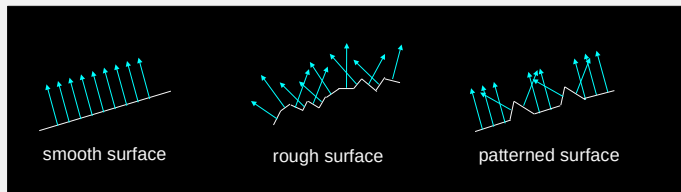


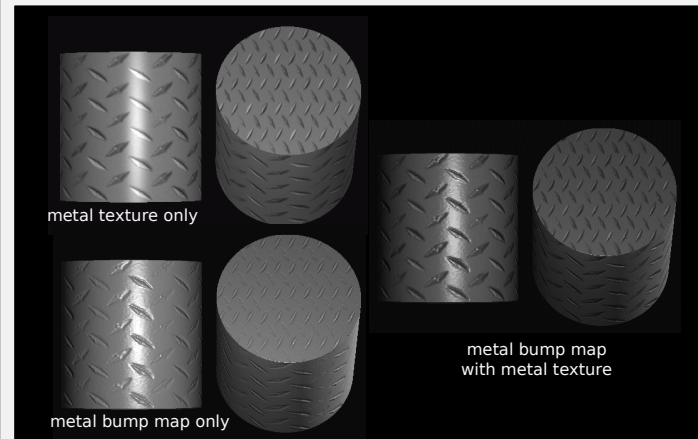
Bump Mapping

the idea: on a rough or patterned surface, surface normals aren't all parallel

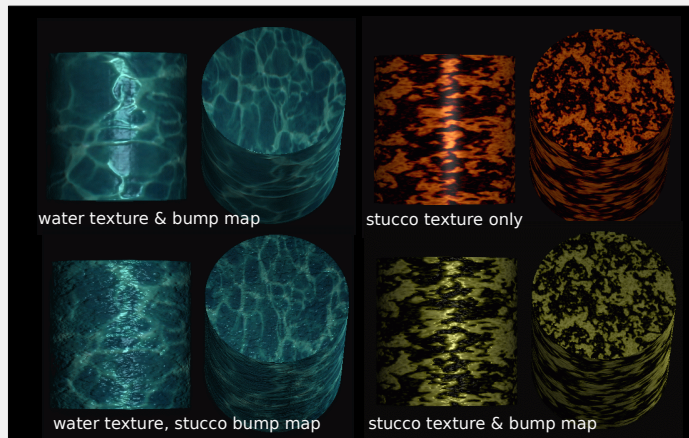


- it is too expensive to actually model a complex surface with polygons, but the effect can be approximated by modeling the smooth surface but perturbing the normals in lighting calculations
- can use textures (as a bump map) to define how to perturb the normals

Examples



Examples

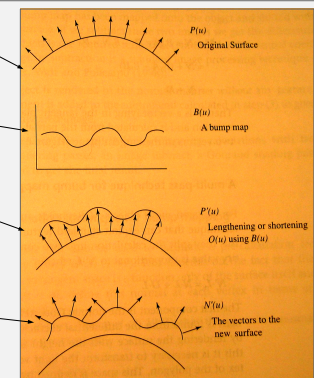


Bump Mapping

idea –

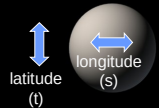
- perturb surface point (the bump)
- compute (an approximate) normal for the perturbed point

- define texture coordinates (u,v) for each point P on the surface
- define bump map $B(u,v)$
(maps points to displacements)
- at each point P on the surface, displace by $B(u,v)$ along the normal at P
 $P' = P + B(u,v) N$
- compute normal N' for P'
- use N' in lighting and other computations



Defining Texture Coordinates

- can use generation techniques previously discussed
- for shapes where there is a convenient parametric representation, use the shrinkwrap approach

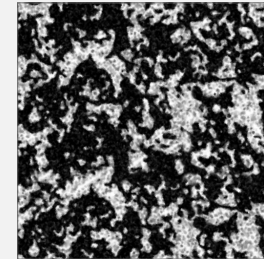
$$\begin{aligned}x &= r \cos(\text{lat}) \sin(\text{long}) \\y &= r \sin(\text{lat}) \\z &= r \cos(\text{lat}) \cos(\text{long})\end{aligned}$$


A diagram of a sphere with a vertical double-headed arrow labeled 'latitude (t)' and a horizontal double-headed arrow labeled 'longitude (s)'.

- for surface point (x,y,z)
 - solve for (r,lat,long)
 - map long \rightarrow u, lat \rightarrow v

Defining the Bump Map

- to reduce computations, obtain bump values via table lookup instead of evaluating a function
- $B(u,v)$ is typically defined by 2D *height field* obtained from a grayscale bitmap image
 - indices u to v are mapped to range [1,255,1,255]



Computing Perturbed Normals

- displaced point

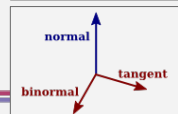
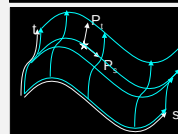
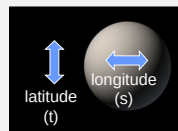
$$P' = P + B(u,v) N$$

- approximation to displaced normal [Blinn 1978]

$$N' = N + B_u (N \times P_t) - B_v (N \times P_s)$$

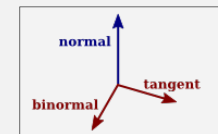
(normalize before use)

- P_s and P_t are the surface tangents along the parameterization axes
 - also known as *tangent* (P_s) and *binormal* (P_t)
- B_u and B_v are the partial derivatives of $B(u,v)$ with respect to u and v , respectively



Computing the Tangent and Binormal

- book's discussion assumes normal and tangent (P_s) are defined as part of the surface
 - suitable when you don't have parametric equations defining the surface (e.g. poly mesh)



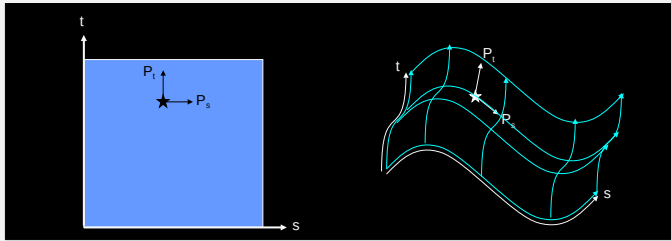
- compute binormal (P_t) as $\text{normal} \times \text{tangent}$

```
vec3 normal = normalize( v_normal );
vec3 tangent = normalize( v_tangent );
vec3 binormal = cross(normal,tangent);
```

Computing the Tangent and Binormal

For surfaces defined by parametric equations –

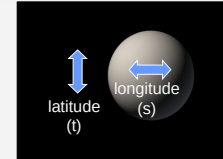
- P_s is partial derivative of P with respect to s
- P_t is partial derivative of P with respect to t
- surface normal at P is the cross product $P_s \times P_t$



Sphere Example

- parametric definition

$$\begin{aligned}x &= r \cos(\text{lat}) \sin(\text{long}) \\y &= r \sin(\text{lat}) \\z &= r \cos(\text{lat}) \cos(\text{long})\end{aligned}$$



- partial derivatives

$$P_s \begin{cases} x' = r \cos(\text{lat}) \cos(\text{long}) \\ y' = 0 \\ z' = -r \cos(\text{lat}) \sin(\text{long}) \end{cases} \quad P_t \begin{cases} x' = -r \sin(\text{lat}) \sin(\text{long}) \\ y' = r \cos(\text{lat}) \\ z' = -r \sin(\text{lat}) \cos(\text{long}) \end{cases}$$

- $N = P_s \times P_t$

$$P_s \times P_t = \begin{bmatrix} r^2 \cos^2(\text{lat}) \sin(\text{long}) \\ r^2 \cos(\text{lat}) \sin(\text{lat}) \cos^2(\text{long}) + r^2 \cos(\text{lat}) \sin(\text{lat}) \sin^2(\text{long}) \\ r^2 \cos^2(\text{lat}) \cos(\text{long}) \end{bmatrix} = r \cos(\text{lat}) \begin{bmatrix} r \cos(\text{lat}) \sin(\text{long}) \\ r \sin(\text{lat}) \\ r \cos(\text{lat}) \cos(\text{long}) \end{bmatrix}$$

— which points in the same direction as (x, y, z)

Computing B_u and B_v

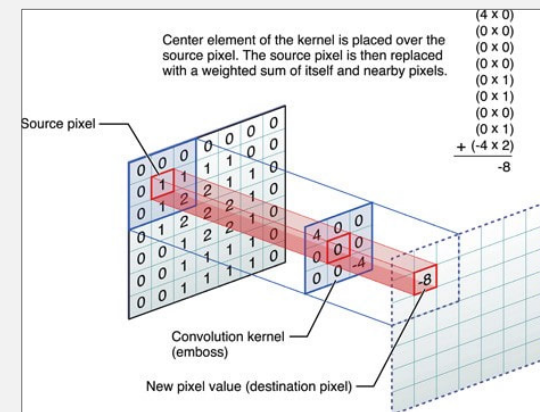
- approximate derivatives B_u and B_v by looking at differences between neighboring entries in bitmap
- obtain B_u by convolving the bump map image with
- obtain B_v by convolving the bump map image with

$$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 0 & -1 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

scale result by range of values in bitmap

Convolution



Computing B_u and B_v

- the book uses a simpler convolution
- obtain B_u by convolving the bump map image with
- obtain B_v by convolving the bump map image with

note: this is opposite what is in the book – this version means that white in the bump map corresponds to a larger distortion outwards

$$\begin{bmatrix} 0 & 1 & -1 \\ -1 & & \\ & 1 & \\ & & 0 \end{bmatrix}$$

```
float bm0 = texture2D( u_bumpmap, v_texCoords ).r;
float bmUp = texture2D( u_bumpmap, v_texCoords + vec2(0.0, 1.0/u_bumpmapSize.y) ).r;
float bmRight = texture2D( u_bumpmap, v_texCoords + vec2(1.0/u_bumpmapSize.x, 0.0) ).r;
vec3 bumpVector = (bm0-bmRight)*tangentI + (bm0-bmUp)*binormalI;
normal += u_bumpmapStrength*bumpVector;
```

scale result by range of values in bitmap
if this is a constant range, can scale by desired strength

tangent and binormal are $(N \times P_t)$ and $(N \times P_s)$, respectively

one pixel up/right
.r = red component of color (same as g, b for grayscale image)

note: normal is still in OC – must convert to EC before using in lighting equation

74

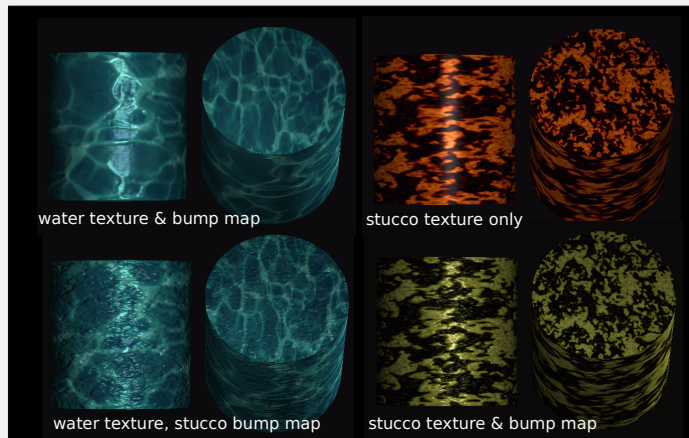
Implementing Bump Mapping

- to compute the perturbed normal N' for OC point (x,y,z)
 - map OC (x,y,z) to TC (u,v)
 - scale TC (u,v) to BC (u',v') – i.e. apply texture transform
 - compute B_u and B_v for (u',v')
 - compute tangent $N \times P_t$ and binormal $N \times P_s$ if needed
 - compute $N' = N + B_u \text{ tangent} - B_v \text{ binormal}$
- use N' instead of regular surface normal for illumination and other lighting-related calculations

CPSC 424: Computer Graphics • Fall 2025

75

Examples



CPSC 424: Computer Graphics • Fall 2025

76